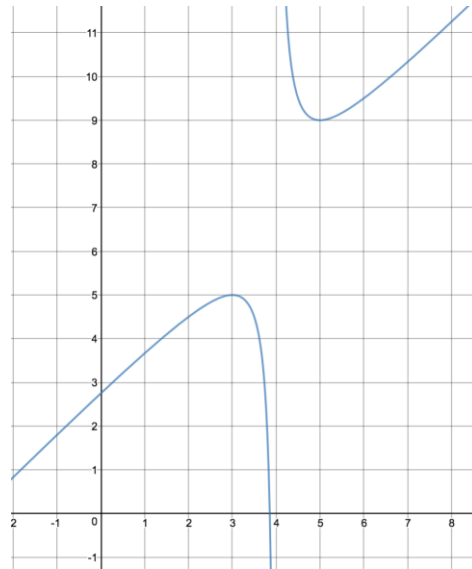
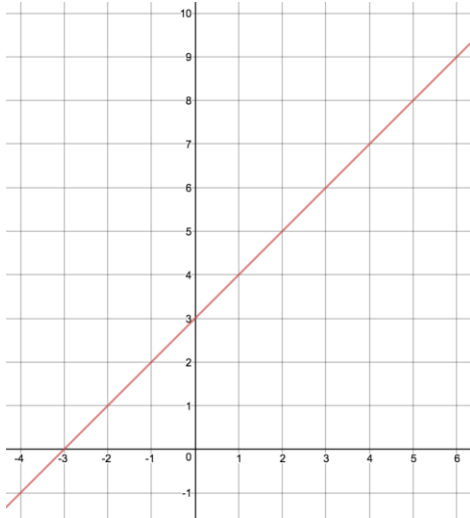


Notes 15.4 Rational Functions: Discontinuities and Limits

$$f(x) = \frac{x^2 - x - 12}{x - 4}$$

$$g(x) = \frac{x^2 - x - 11}{x - 4}$$

Do the graphs of these similar equations look alike? They are each undefined at  $x = \underline{\hspace{2cm}}$  or have a **discontinuity**.



Since the factor  $(x - 4)$  can be removed, it is called a **removable discontinuity**.

no factors can be removed from  $g(x)$  so there is a **vertical asymptote**

As  $x$  approaches 4,  $f(x)$  approaches  $\underline{\hspace{2cm}}$ .

$g(4) =$

$\lim_{x \rightarrow 4} f(x) = \underline{\hspace{2cm}}$  This # is called the **limit**.

The **limit**  $\lim_{x \rightarrow 4} g(x) =$

$$f(x) = \frac{x^3 - 5x^2 + 8x - 6}{x - 3}$$

$$g(x) = \frac{x^3 - 5x^2 + 8x - 5}{x - 3}$$

Where is the **discontinuity**?

Find the **limit** of each function at the discontinuity.