

Notes 2.1 Antiderivatives (Indefinite Integrals)

• Reversing the operation of finding a derivative is called antiderivative.
 $f(x) = x^2 + 3$ and $f'(x) = 2x$ In words, the antiderivative of $2x$ is $x^2 + C$

• We use the integral sign \int for this operation called integration.
 $\int 2x \, dx = x^2 + C$

$\int x^n \, dx = \frac{x^{n+1}}{n+1} + C$ increase the exponent by 1, then divide by the new exponent.

$$\int x^{-1} \, dx = \ln |x| + C$$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int e^{ax} \, dx = \frac{1}{a} e^{ax} + C$$

Find the following indefinite integrals by Integrating.

1. $\int x \, dx$

2. $\int 6x \, dx$

3. $\int 5 \, dx$

4. $\int 8x^5 \, dx$

5. $\int \frac{1}{x^3} \, dx$

6. $\int x^{-1} \, dx$

7. $\int (12u^2 - 8u + 5) \, du$

8. $\int (3t + 5)^2 \, dt$

$$\int \sin ax \, dx = -\frac{1}{a} \cos ax + C$$

$$\int \cos ax \, dx = \frac{1}{a} \sin ax + C$$

$$\int e^{ax} \, dx = \frac{1}{a} e^{ax} + C$$

9. $\int \sin 3x \, dx$

10. $\int \cos 5x \, dx$

11. $\int e^{3t} \, dt$