## Section 9-8 Mathematical Expectation

At a school carnival, students are awarded points for winning games. At the end of the evening, they may trade in points for prizes. You roll a single die. (game is 50 points to play) Payoffs are:

| Number | Probability | Points won(payoff) | Mathematical Expectation |
| :--- | ---: | :--- | :--- |
| 1 | $1 / 6$ | -50 |  |
| 2 | $1 / 6$ | 10 |  |
| 3 | $1 / 6$ | -50 |  |
| 4 | $1 / 6$ | 10 |  |
| 5 | $1 / 6$ | -50 |  |
| 6 | $1 / 6$ | 100 |  |

This is why some games are rigged at carnivals and casinos!

## Mathematical Expectation

is found by multiplying the probability by the payoff and adding them.
$\mathrm{E}=\sum P\left(A_{1}\right) a_{1}+P\left(A_{2}\right) a_{2}+P\left(A_{3}\right) a_{3}+P\left(A_{4}\right) a_{4} \ldots P\left(A_{n}\right) a_{n}$

- For the mutually exclusive events $A_{1}, A_{2}, A_{3}, \ldots, A_{n}$ in the experiment.
- The values $a_{1}, a_{2}, a_{3}, \ldots, a_{n}$ correspond to the outcomes of $A_{1}, A_{2}, A_{3}, \ldots, A_{n}$

It is the weighted average for a random experiment each time it is run.

| Skeeball |
| :--- |
| $P(10)=0.5$ |
| $P(20)=0.25$ |
| $P(30)=0.15$ |
| $P(40)=0.07$ |
| $P(50)=0.03$ |

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