

Pre-Cal. --- Chapter 5 Review

Key

1. Express $\sin 3x + \sin 7x$ as a product of sines and/or cosines of positive multiples of x .

$$2 \sin \frac{1}{2}(3x+7x) \cos \frac{1}{2}(3x-7x)$$

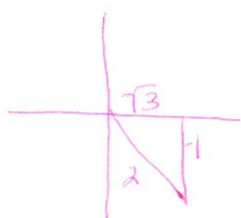
$$2 \sin \frac{1}{2}(10x) \cos \frac{1}{2}(-4x)$$

$$2 \sin 5x \cos(-2x)$$

$$2 \sin 5x \cos 2x$$

2. Draw a sketch and use it to express $\sqrt{3} \cos x - \sin x$ as a single cosine with a phase displacement.

* radians



$$y = 2 \cos(x + 0.5236)$$

3. Use the result from #2 to solve: $\sqrt{3} \cos x - \sin x = 1.5$

$$1.5 = 2 \cos(x + 0.5236)$$

$$.75 = \cos(x + 0.53)$$

$$\pm \cos^{-1}(.75) + 2\pi n = x + 0.53$$

$$-0.53 \pm .728 + 2\pi n = x$$

$$x = .198$$

$$x = -1.258$$

4. Transform this product into a sum: $y = 2 \cos 19x \cos x$

$$= \cos(19x+x) + \cos(19x-x)$$

$$= \cos 20x + \cos 18x$$

5. Solve $\cos 2\theta + \cos \theta = 1$ algebraically for $\theta \in [-100^\circ, 850^\circ]$. (Transform $\cos 2\theta$ so that it involves only $\cos \theta$.)

$$2 \cos^2 \theta - 1 + \cos \theta = 1$$

$$2 \cos^2 \theta + \cos \theta - 2 = 0$$

$$\cos \theta = -1.28$$

$$\cos \theta = .78$$

$$\theta = \pm \cos^{-1}(.78) + 360^\circ n$$

$$\theta = \pm 38.74^\circ + 360^\circ n$$

$$38.74^\circ, 398.74^\circ, 758.74^\circ$$

$$-38.74^\circ, 321.26^\circ, 681.26^\circ$$

6. Use the double argument property, $\cos 2x = 1 - 2 \sin^2 x$, to express $\cos 120^\circ$ in terms of $\sin 60^\circ$.

$$\frac{2x}{2} = \frac{120^\circ}{2}$$

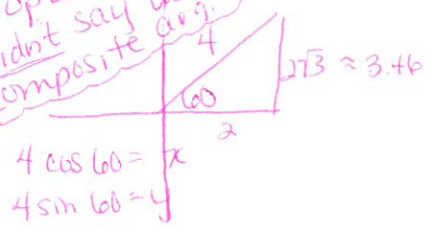
$$x = 60^\circ$$

$$\cos 120^\circ = 1 - 2 \sin^2(60^\circ)$$

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7. Use the composite argument property for cosine to transform $y = 4 \cos(\theta - 60^\circ)$ to a linear combination of $\cos \theta$ and $\sin \theta$.

Option if it didn't say "use composite arg."

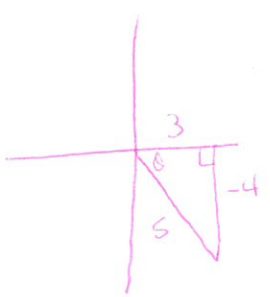


$$y = 4(\cos \theta \cos 60^\circ + \sin \theta \sin 60^\circ)$$

$$y = 4(.5 \cos \theta + .866 \sin \theta)$$

$$y = 2 \cos \theta + 3.46 \sin \theta$$

8. If $\sin \theta = \frac{-4}{5}$, and $\theta \in [270^\circ, 360^\circ]$, find $\sin 2\theta$ and $\sin \frac{\theta}{2}$.



$$\sin 2\theta = 2 \sin \theta \cos \theta$$

$$= 2 \left(\frac{-4}{5}\right) \left(\frac{3}{5}\right)$$

$$= \frac{-24}{25}$$

$$\sin \frac{\theta}{2} = \pm \sqrt{\frac{1 - \cos \theta}{2}}$$

$$= \pm \sqrt{\frac{1 - \frac{3}{5}}{2}}$$

$$= \pm \sqrt{\frac{\frac{2}{5}}{2}}$$

$$= \pm \sqrt{\frac{1}{5}}$$

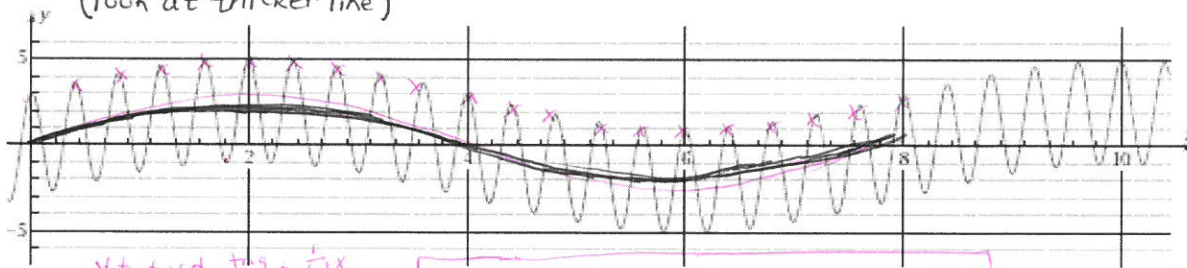
$$= \pm \frac{1}{\sqrt{5}}$$

$A \Rightarrow 270 - 360$
 $\frac{1}{2}A \Rightarrow 135 - 180$
(2nd quad.)

$$\frac{1}{\sqrt{5}} \text{ or } \frac{\sqrt{5}}{5}$$

9. Write the equation for the following graphs:

(look at thicker line)



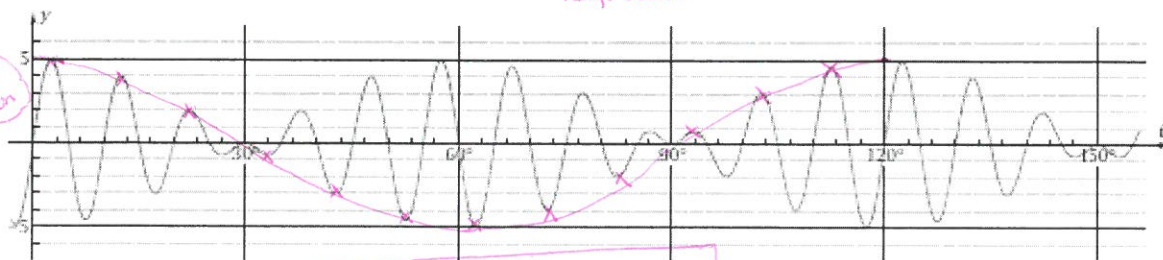
$v_t + v_d \frac{1}{\text{period}} \frac{1}{\text{hd}} x$
 $2\pi \times \text{hd} = 8 \quad \text{hd} = \frac{8}{2\pi}$

$$y = 2 \sin \frac{\pi}{4} x + 3 \cos 5\pi x$$

large curve

$$20 \cdot \frac{\pi}{4} = \frac{20\pi}{4}$$

odd function



$360 \times \text{hd} = 120$
 $\text{hd} = \frac{120}{360}$

$$y = 5 \cos 3\theta \cdot \sin 36\theta$$