

Writing Circle and Ellipse Equations

General parametric equation for an ellipse:
 (h, k) is center of the ellipse $x = h + a \cos T$
 a is the x-radius $y = k + b \sin T$
 b is the y-radius

* For Circle $a = b$

* Ellipse

1. $x = 6 + 5 \cos T$ center (6, -3)
 $y = -3 + 2 \sin T$ x rad = 5 y rad = 2

+ $\left(\frac{x-6}{5}\right)^2 = (\cos T)^2$
 + $\left(\frac{y+3}{2}\right)^2 = (\sin T)^2$
 cartesian $\left(\frac{x-6}{5}\right)^2 + \left(\frac{y+3}{2}\right)^2 = 1$

Write parametric equations.

3. $\left(\frac{x-2}{5}\right)^2 + \left(\frac{y-4}{2}\right)^2 = 1$

$x = 2 + 5 \cos T$
 $y = 4 + 2 \sin T$

* Circle

2. $x = -1 + 4 \cos T$ center (-1, 0)
 $y = 4 \sin T$ x rad = 4 y rad = 4

+ $\left(\frac{x+1}{4}\right)^2 = (\cos T)^2$
 + $\left(\frac{y}{4}\right)^2 = (\sin T)^2$
 $\left(\frac{x+1}{4}\right)^2 + \left(\frac{y}{4}\right)^2 = 1$

4. $\left(\frac{x-6}{3}\right)^2 + \left(\frac{y+1}{3}\right)^2 = 1$

$x = 6 + 3 \cos T$
 $y = -1 + 3 \sin T$

Circle equation when $a=b$ and Ellipse equation a is major radius and b is minor radius
 $\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$ $\frac{(x-h)^2}{b^2} + \frac{(y-k)^2}{a^2} = 1$

Write a Cartesian equation that satisfies each set of conditions.

5. circle with center (8, -3) radius = 6

$\left(\frac{x-8}{6}\right)^2 + \left(\frac{y+3}{6}\right)^2 = 1$ or $(x-8)^2 + (y+3)^2 = 36$

6. circle with center (-5, 2), passes through (-9, 6)

$(x-h)^2 + (y-k)^2 = r^2$
 $(-9+5)^2 + (6-2)^2 = r^2$
 $16 + 16 = r^2$
 $\sqrt{32} = r$
 $4\sqrt{2} = r$

OR

$\left(\frac{x+5}{\sqrt{32}}\right)^2 + \left(\frac{y-2}{\sqrt{32}}\right)^2 = 1$
 $(x+5)^2 + (y-2)^2 = 32$

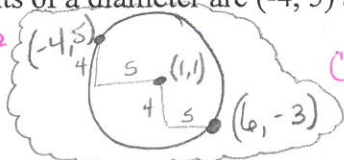
7. circle whose endpoints of a diameter are $(-4, 5)$ and $(6, -3)$

$$(-4-1)^2 + (5-1)^2 = r^2$$

$$25 + 16 = r^2$$

$$\sqrt{41} = r$$

center $\rightarrow \left(\frac{-4+6}{2}, \frac{5-3}{2} \right) = (1, 1)$

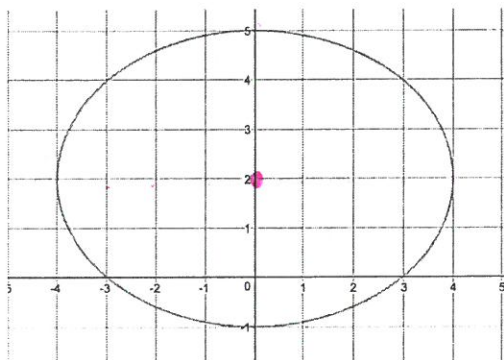


$$\left(\frac{x-1}{\sqrt{41}} \right)^2 + \left(\frac{y-1}{\sqrt{41}} \right)^2 = 1$$

$$(x-1)^2 + (y-1)^2 = 41$$

Write the equation

8.



center $(0, 2)$

x rad = 4

y rad = 3

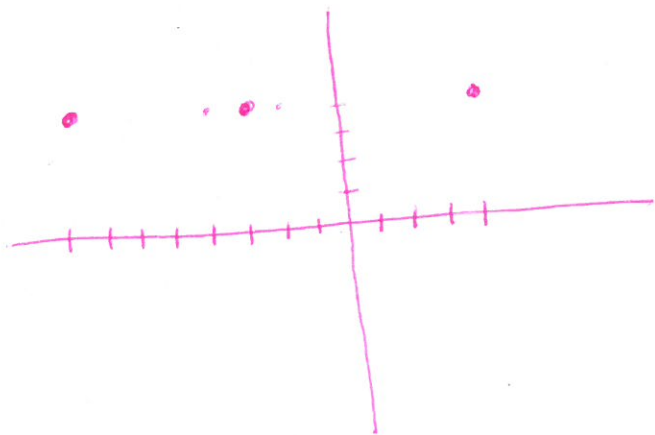
$$\left(\frac{x-0}{4} \right)^2 + \left(\frac{y-2}{3} \right)^2 = 1$$

OR

$$x = 4 \cos T$$

$$y = 2 + 3 \sin T$$

9. ellipse whose endpoints of major axis are $(-8, 4)$ and $(4, 4)$, foci at $(-3, 4)$ and $(-1, 4)$



$$\frac{-8+4}{2} = -2 \quad \text{center } (-2, 4)$$

$$a = 6$$

$$c = 1$$

$$a^2 = b^2 + c^2$$

$$36 - 1 = b^2 \quad b = \sqrt{35}$$

$$\left(\frac{x+2}{6} \right)^2 + \left(\frac{y-4}{\sqrt{35}} \right)^2 = 1$$